

# Deer Population

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# Introduction

- NC deer population is about 1,000,000
- Current population can be modeled by:

$$N_{t+1} = N_t + 0.12\left(1 - \frac{N_t}{1,200,000}\right)N_t$$

- growth rate: 12%      carrying capacity: 1,200,000
- Population is nearing its carrying capacity

# Introduction Continued

- If the state introduces a predator, populations can be modeled by:

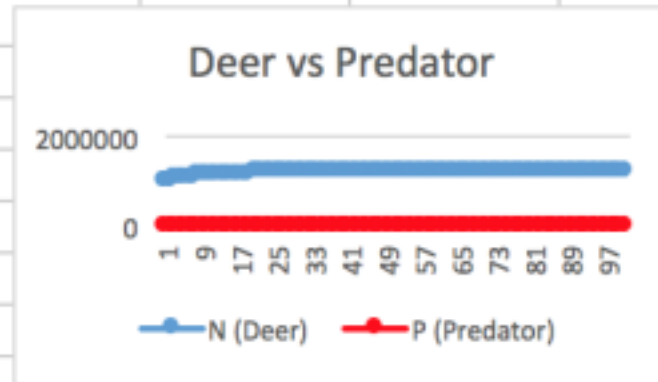
$$N_{t+1} = N_t + 0.12\left(1 - \frac{N_t}{1,200,000}\right)N_t - \frac{cN_tP_t}{a + N_t}$$

$$P_{t+1} = P_t + \frac{bN_tP_t}{a + N_t} - mP_t$$

- a, b, and c can be values larger than 1
- m must be a value between 0 and 1 because it's a mortality rate

# Excel

A	B	C	D	E	F	G	H
t (Time)	N (Deer)	P (Predator)		a	b	c	m
0	1000000	1000		0.1	0.1	0.1	0.1
1	1019900	999.99999					
2	1038168.4	999.99998					
3	1054869.24	999.999971					
4	1070078.64	999.999961					
5	1083881.25	999.999952					
6	1096367.14	999.999943					
7	1107629.11	999.999933					
8	1117760.38	999.999924					

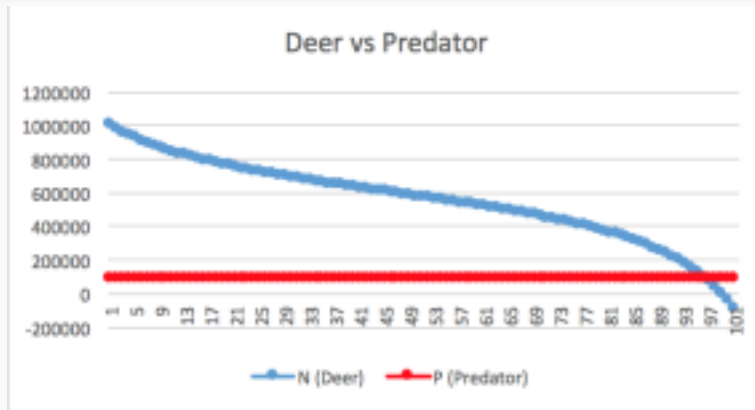


$$f_x = B2 + (0.12 * (1 - (B2 / 1200000)) * B2) - (\$G\$2 * B2 * C2 / (\$E\$2 + B2))$$

$$f_x = C2 + (\$F\$2 * B2 * C2 / (\$E\$2 + B2)) - (\$H\$2 * C2)$$

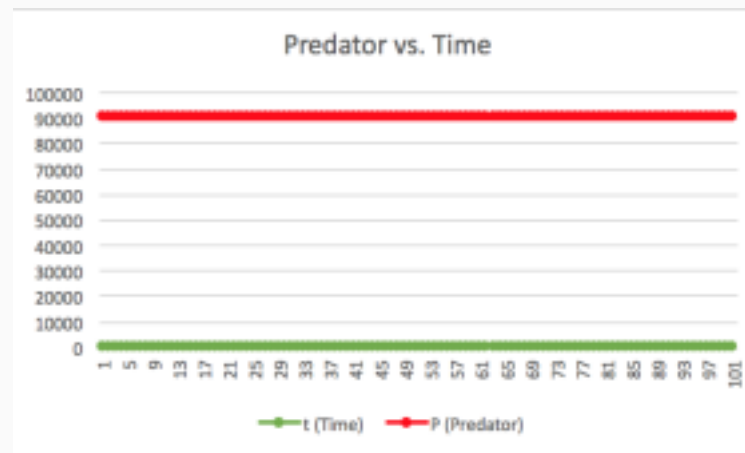
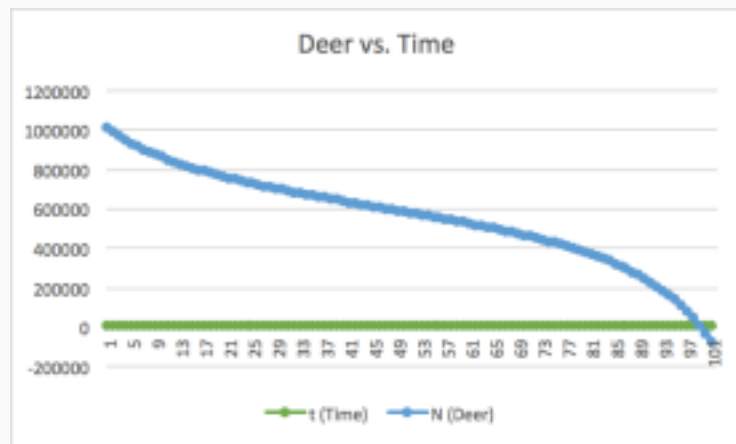
- $N(0) = 1,000,000$
- 100-year time frame

# Population Goes Extinct

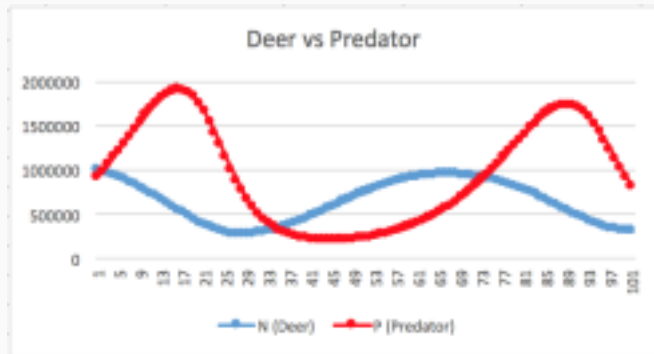


t (Time)	N (Deer)	P (Predator)	a	b	c	m
0	1000000	90000		0.001	0.9	0.459
						0.9

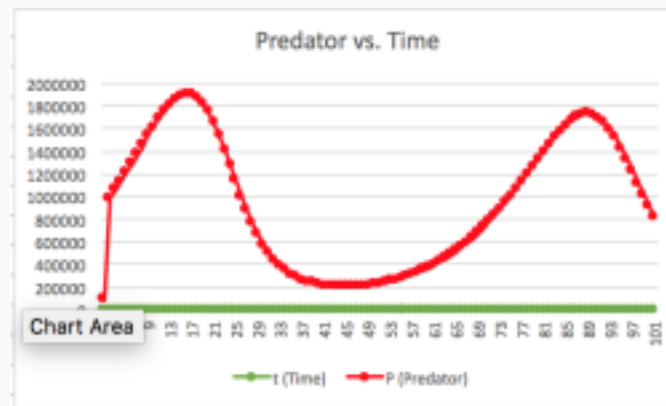
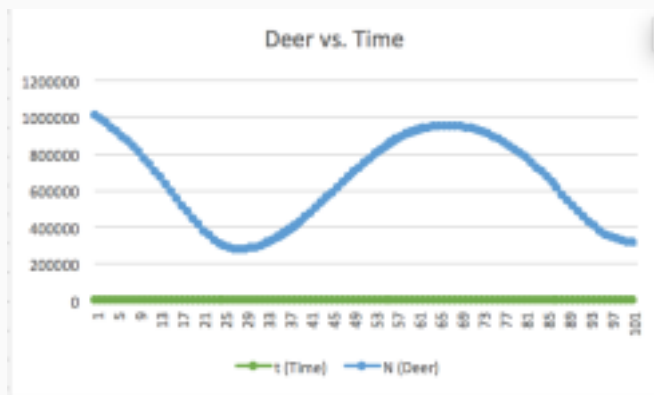
- a doesn't matter
- b & m are the same value while c is relatively smaller



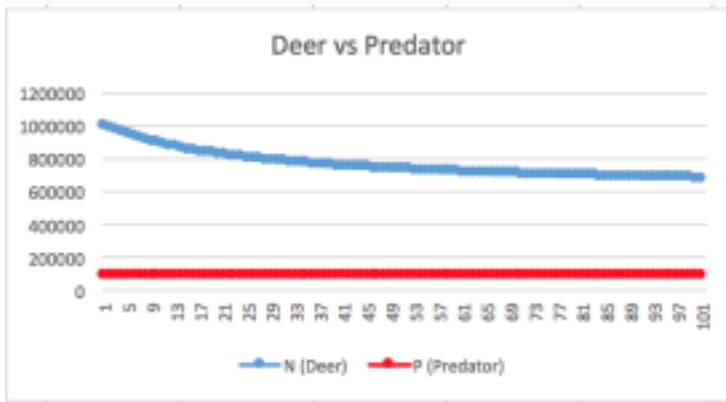
# Cycling Population



t (Time)	N (Deer)	P (Predator)	a	b	c	m
0	1000000	917847	160000	0.9	0.05	0.7

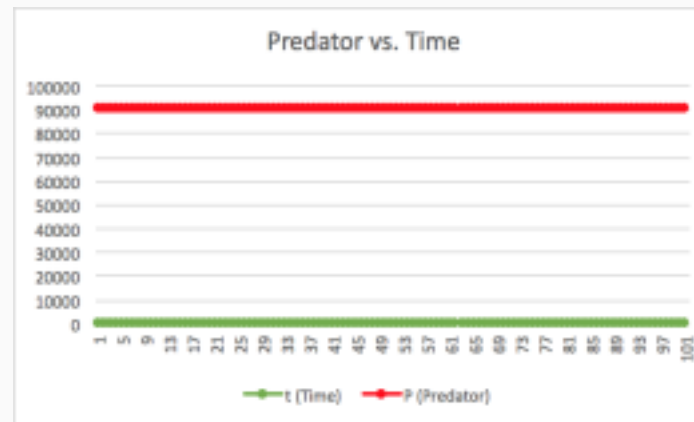
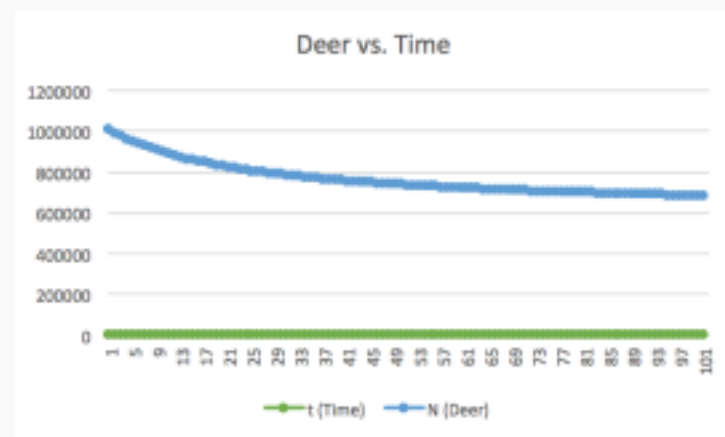


## Population Kept Under 700,000 Deer



t (Time)	N (Deer)	P (Predator)	a	b	c	m
0	1000000	90000	0.001	0.2	0.4	0.2

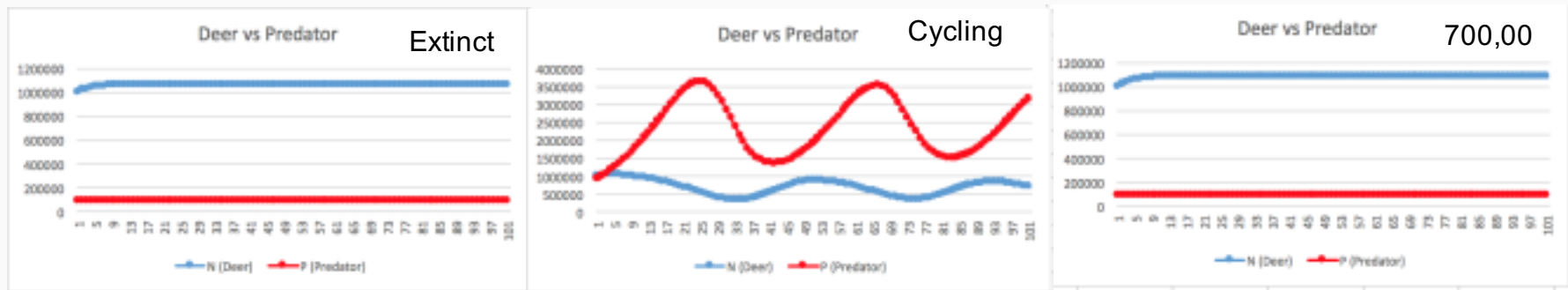
- a doesn't matter
- b & m are the same values (small) while c is relatively larger



## Stochastic Deer Growth Rate Changes

Change growth rate to equally likely values:  $H_i = 0.34$ ,  $Mid = 0.12$  (the same),  $Lo = -0.1$

Hi:



Lo:

